JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD
B.Tech II Year II Semester Examinations, November/December - 2015 DESIGN AND ANALYSIS OF ALGORITHMS
(Information Technology)
Time: 3 Hours
Max. Marks: 75
Note: This question paper contains two parts A and B.
Part A is compulsory which carries 25 marks. Answer all questions in Part A.
Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions.

## PART- A

1.a) Explain the properties of an algorithm.
b) Write an algorithm of weighted union. [3M]
[2M]
c) What are the applications of minimum cost spanning tree. [2M]
d) Write an algorithm of greedy knapsack. [3M]
e) Explain how dynamic programming is useful to solve 0/1 Knapsack. [2M]
f) Explain the importance of all pairs shortest path problem. [3M]
g) Find the sum of sets for the following set of integers by fixed tuple. $\{1,2,3,5,6,7,8,9,10\}$ for $W=8$.
[2M]
h) What is meant by branch and bound.
i) Write a nondeterministic search algorithm.
j) Distinguish between P and NP.

## PART-B

2.a) Solve the recurrence: $T(n)=4 T(n / 2)+n$, Where $n \geq 1$ and is a power of 2 .
b) Write an algorithm for the finding the GCD of two numbers and also find the time complexity of the same.

## OR

3.a) Write an algorithm of Fibonacci of $n$ given numbers and also find its Complexity.
b) Explain the asymptotic notations with an example.
4. Explain the prim's and Kruskal's algorithms.

## OR

5.a) Write a control abstraction for the subset parading using greedy method.
b) What is the solution generated by using job sequencing with deadlines when $\mathrm{n}=7$, (P1, P2, P3 .....P7) $=(3,5,20,18,1,6,30)$, and $(\mathrm{d} 1, \mathrm{~d} 2, \ldots . . \mathrm{d} 7)=(1,3,4,3,2,1,2)$.
6.a) Solve the travelling sales person problem by using the dynamic programming.

b) Write an algorithm of OBST.

## OR

7. Consider 4 elements $\mathrm{al}<\mathrm{a} 2<\mathrm{a} 3<\mathrm{a} 4$ with
$\mathrm{q}(0)=\frac{1}{8}, \mathrm{q}(1)=\frac{1}{16}, \mathrm{q}(2)=\mathrm{q}(3)=\mathrm{q}(4)=\frac{1}{16}: \mathrm{p}(1)=\frac{1}{4}, \mathrm{p}(2)=\frac{1}{8}, \mathrm{p}(3)=\mathrm{p}(4)=\frac{1}{16}$.
Construct the table of values of $\mathrm{W}(\mathrm{i}, \mathrm{j}), \mathrm{R}(\mathrm{i}, \mathrm{j})$ and $\mathrm{C}(\mathrm{i}, \mathrm{j})$ computed by the algorithm to compute the roots of optimal sub trees.
8.a) Draw the portion of the state space tree generated by LCBB for the following knapsack instances: $\mathrm{n}=5,\left(\mathrm{P}_{1}, \mathrm{P}_{2}, \mathrm{P}_{3}, \mathrm{P}_{4}, \mathrm{P}_{5}\right)=(10,15,6,8,4)$,

$$
\begin{equation*}
\left(W_{1}, W_{2}, W_{3}, W_{4}, W_{5}\right)=(4,6,3,4,2) \text { and } m=12 \tag{5+5}
\end{equation*}
$$

b) Explain in detail how the technique of backtracking can be applied to solve the 8 -queens problem.

## OR

9. Consider the traveling sales person instance defined by the cost matrix

$$
\left[\begin{array}{lllll}
\infty & 7 & 3 & 12 & 8 \\
3 & \infty & 6 & 14 & 9 \\
5 & 8 & \infty & 6 & 18 \\
9 & 3 & 5 & \infty & 11 \\
18 & 14 & 9 & 8 & \infty
\end{array}\right]
$$

a) Obtain the reduced cost matrix
b) Obtain the state space tree that will be generated by LCBB. Label each node by its $\hat{C}$ value. Write out the reduced matrices corresponding to each of these nodes.
[5+5]
10. Explain 0/1 knapsack problem and cook's theorem.

## OR

11.a) Show that the Hamiltonian cycle problem is reducible to the traveling sales person problem (Choose either directed or undirected graphs for both problems).
b) Explain non-deterministic algorithms.

