**R16** 

## Code No: 133BC

## JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B.Tech II Year I Semester Examinations, May/June - 2019 MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE (Common to CSE, IT)

Time: 3 Hours Max. Marks: 75

**Note:** This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit.

Each question carries 10 marks and may have a, b, c as sub questions.

## **PART-A**

(25 Marks) [2]

- 1.a) Find the negative of  $p \rightarrow q$ .
  - b) Test the validity of the following argument

 $p \wedge r \rightarrow \neg q, \neg q \rightarrow r : p \wedge r \rightarrow r$  [3]

- c) If  $f(x) = x^2 6 = y$ , then find  $f^{-1}(y)$ . [2]
- d) If  $f: G_1 \to G_2$  is a homorphism and  $a \in G$  then prove that  $[f(a)]^{-1} = f(a^{-1})$ . [3]
- e) How many 5 digit numbers are possible, which are greater than 40000 with the digits 1, 2, 3, 4, 5. [2]
- f) Find the number of positive integer solutions of x + y + z = 12. [3]
- g) Solve the recurrence relation  $u_{n+2} u_{n+1} 6u_n = 0$ . [2]
- i) If the adjacency matrix of the Graph is  $\begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \end{bmatrix}$ , then draw the graph. [2]
- j) If G is a k regular graph with 18 edges and the order of the graph is 9. Find the value of k. [3]

## PART - B

(50 Marks)

2.a) Test the validity of the following argument.

If I study, I will not fail in the examination.

If I do not watch TV in the evenings, I will study.

I failed in the examination.

Therefore I must watch TV in the evenings.

b) Prove that the following argument is valid.

$$\neg \exists x (p(x) \land q(x))$$

p(a)

$$\therefore \neg q(a)$$
 [5+5]

OR

- 3.a) Prove that  $(p \uparrow q) \rightarrow r$  and  $(p \land q) \lor r$  are logically equivalent.
  - b) Prove that the following argument is valid.

$$\forall x p(x) \rightarrow \neg q(x)$$

$$\neg \exists x ((r(x) \lor s(x)) \land \neg q(x))$$

r(a)

$$\therefore \neg p(a)$$
 [5+5]

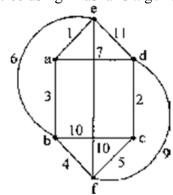
- 4.a) Let  $X=\{1,2,3\}$  and f, g, h and s be functions from X to X given by  $f=\{(1,2), (2,3), (3,1)\}$ ,  $g=\{(1,2), (2,1), (3,3)\}$  h= $\{(1,1), (2,2), (3,1)\}$  Find fog, fohog.
  - b) If  $f: G_1 \to G_2$  is an isomorphism, then prove that  $f^{-1}: G_2 \to G_1$  is also an isomorphism. [5+5]

OR

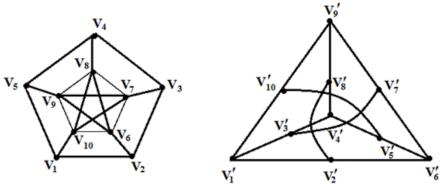
- 5.a) Prove that the relation a congruent to b mood H is an equivalence relation.
  - b) Prove that the set of even integers forms a group under addition. [5+5]
- 6.a) Find the number of solutions of  $x_1+x_2+x_3=19$  with the condition  $x_1>1$ ,  $x_2>2$ ,  $x_3>1$ .
  - b) Prove that if 11 integers are selected from among  $\{1, 2, ... 20\}$ , then the selection includes integer a and b such that a b = 2. [5+5]

OR

- 7.a) Find the number of integers < 250 and divisible by 3 or 5 or 11.
  - b) Suppose 14 students in a class appear at a university examination. Prove that there exists at least two among them whose seat number differ by a multiple of 13. [5+5]
- 8. Solve the recurrence relation.  $u_n 2u_{n-1} 3u_{n-2} = 5^n$ ,  $n \ge 2$ ,  $u_0 = 1$ ,  $u_1 = 1$  [10]
- 9. Solve the recurrence relation using generating function.  $u_{n+2} 2u_{n+1} + u_n = 2^n$ ,  $u_0 = 2$ ,  $u_1 = 1$ . [10]
- 10.a) Suppose that G is a non directed graph with 12 edges. Suppose that G has 6 vertices of degree 3 and the rest have degree less than 3. Determine the minimum number of vertices G can have.
  - b) Find the minimal spanning tree using Krushal's algorithm. [5+5]



11.a) Show that the following graphs are isomorphic.



b) Prove that a graph G with at least one edge is 2-chromatic if and only if G has no cycle of odd length. [5+5]

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