## Code No: 133BC

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

# B.Tech II Year I Semester Examinations, December - 2019 MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE (Common to CSE, IT) 

Time: 3 Hours
Max. Marks: 75
Note: This question paper contains two parts A and B.
Part A is compulsory which carries 25 marks. Answer all questions in Part A.
Part B consists of 5 Units. Answer any one full question from each unit.
Each question carries 10 marks and may have a, b, c as sub questions.
PART- A
(25 Marks)
1.a) Define a statement and give an example.
b) Explain Connectives with suitable example.
c) What is an Algebraic Structure and give an example.
d) Differentiate between Binary relation and equivalence relation.
e) Compare between Combinations and Permutations with appropriate example.
f) What is the Principle of Inclusion Exclusion in elementary Combinatorics.
g) What is recurrence relation and give an example?
h) Find the coefficient for the generating function $2^{1}, 2^{2}, 2^{3}, 2^{4} \ldots$.
i) Define Isomorphism in Graphs with suitable example.
j) Briefly write about Trees Properties.

## PART-B

(50 Marks)
2.a) Identify the converse, inverse and contra positive for the Proposition $\mathrm{P} \rightarrow \mathrm{Q}$.
b) Find DNF of $\mathrm{P} \rightarrow((\mathrm{P} \rightarrow \mathrm{Q}) \wedge \sim(\sim \mathrm{Q} \vee \sim \mathrm{P}))$

## OR

3.a) Differentiate between PDNF and PCNF with two examples.
b) Identify whether $(\mathrm{P} \vee \mathrm{Q}) \vee \sim \mathrm{R}$ is a tautology or not.
4.a) Define Lattice and explain its properties.
b) If $\mathrm{a}, \mathrm{b}$ are any two elements of a group ( $\mathrm{G},$. ) which commute, show that $\mathrm{a}^{-1}$ and b commute, $\mathrm{b}^{-1}$ and a commute, $\mathrm{a}^{-1}$ and $\mathrm{b}^{-1}$ commute.

## OR

5.a) Define abelian group with example.
b) Construct the Hasse diagram for the divisibility relation $A=\{3,6,12,36,72\}$.
6.a) Predict that in how many ways two slices of pizza can be chosen from a plate containing one slice each of pepperoni, sausage, mushroom, and cheese pizza?
b) If a person having 4 trousers and 3 shirts, then identify the number of ways of selecting a pair?

## OR

7.a) How many ways are there to place 20 identical balls into 6 different boxes in which exactly 2 boxes are empty?
b) State and explain Binomial theorem with an example.
8.a) Solve the recurrence relation $\mathrm{a}_{\mathrm{n}}-6 \mathrm{a}_{\mathrm{n}-1}+8 \mathrm{a}_{\mathrm{n}-2}=9, \mathrm{n}>=2, \mathrm{a}_{0}=10, \mathrm{a}_{1}=25$ by using generating function?
b) Solve the recurrence relation $a_{n}-a_{n-1}+16 a_{n-2}+34 a_{n-3}=1, n>=2, a_{0}=0, a_{1}=2, a_{2}=6$.

## OR

9.a) Solve the recurrence relation $a_{n}-2 a_{n}-1+8 a_{n}-2=0 n>=2, a_{0}=5, a_{1}=31$.
b) Solve the recurrence relation $\mathrm{a}_{\mathrm{n}+1}=8 \mathrm{a}_{\mathrm{n}}, \mathrm{n}>=0$ where $\mathrm{a}_{0}=4$.
10.a) Discuss and differentiate between Euler graph and Euler Circuits.
b) Briefly discuss about spanning Trees with appropriate illustration.

OR
11.a) Differentiate between Hamiltonian Graphs and Euler circuits.
b) Write applications of graph theory.

