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S.E. (E&TC/Electronics) (First Semester) EXAMINATION, 2017

SIGNALS AND SYSTEMS

(2012 PATTERN)

Time : Two Hours

Maximum Marks : 50

- N.B. :—** (i) Attempt *four* questions, Q. 1 or Q. 2, Q. 3 or Q. 4, Q. 5 or Q. 6, Q. 7 or Q. 8.
- (ii) Figures to the right indicate full marks.
- (iii) Assume suitable data, if necessary.
- (iv) Neat diagrams should be drawn wherever necessary.
- (v) Use of electronic non-programmable calculator is allowed.

1. (a) Find the time shifted signal : [4]

$$y[n] = x[n + 4]$$

$$x[n] = \begin{cases} 1 & n = 1, 3 \\ -1 & n = -1, -2 \\ 0 & n = 0, 2 \end{cases}$$

- (b) Find whether the following signals are periodic or not. If periodic, calculate the fundamental period : [4]

(i) $x[t] = \sin 200 \pi t + 2 \cos 100 \pi t$

(ii) $x[n] = \sin \frac{62n}{10}$

P.T.O.

- (c) Determine whether the following system is Static/Dynamic, Linear/non-linear causal/non-causal and stable/unstable [4]

$$y(t) = x^2(t).$$

Or

2. (a) Determine and sketch, even and odd components of the following signals : [4]

(i) $x[n] = e^{-(n/4)} u[n]$

(ii) $x(t) = 1, 0 \leq t \leq 4.$

- (b) Determine whether the following signals are energy signals, power signals or neither : [4]

(i) $x(t) = e^{-at} u(t), a > 0$

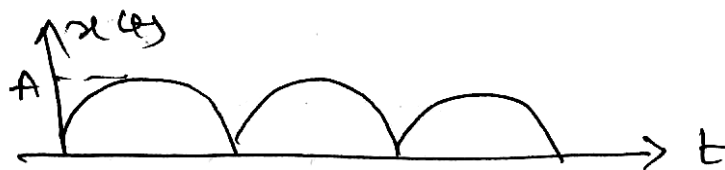
(ii) $x(t) = t.u(t).$

- (c) Determine the stability and causality for the LTI system with the following impulse responses : [4]

(i) $h(t) = e^{-t}u(t - 1)$

(ii) $h[n] = \cos [n]u[n].$

3. (a) Find the quadrature Fourier series for the full wave rectified sine wave as shown in Fig. [6]



(b) Using properties of Laplace transform, find : [6]

(i) $x(3t)$

(ii) $x(t - 2)$, if $X(s) = \frac{2s}{s^2 + 2}$.

Or

4. (a) Calculate Laplace transform of $x(t) = e^{-2t} u(t) - e^{2t} u(-t)$ and plot ROC. [6]

(b) Find initial and final value of : [6]

(i) $X(s) = \frac{0.8}{s(s^2 + 0.6s + 0.2)}$

(ii) $\frac{1}{s+1}$.

5. (a) Find the following for the given signal $x(t)$: [6]

(i) Autocorrelation

(ii) Energy from $x(t)$ and Autocorrelation

(iii) Energy spectral density $x(t) = e^{-4t} .u(t)$.

(b) Define energy spectral density and prove relation between Autocorrelation and ESD. [4]

(c) Plot the correlogram for the sequences $x[n]$ and $y[n]$ given below :
 $x[n] = u[n]$; $y[n] = u[n - 4]$. [3]

Or

6. (a) State and describe properties of Autocorrelation function of CT energy signals. [6]

(b) Find the cross correlation by analytical method of the following signals : [7]

$$x_1[n] = \{4, 3, 2, 1\}, x_2[n] = \{3, 2, 1, -1\}.$$

↑

7. (a) Probability Density Function (PDF) of a random variable X is given by : [7]

$$f_x(\mathbf{X}) = \begin{cases} k(1 - \mathbf{X}^2) & 0 \leq \mathbf{X} \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

Then find (1) k (2) CDF (3) $P(0 \leq \mathbf{X} \leq 2)$.

- (b) There are four white shirts and five black shirts inside a bag. What is the probability of drawing a white shirt from a bag ? [4]
- (c) State the significance of standard deviation. [2]

Or

8. (a) State the properties of probability distribution function. [6]
- (b) With example, explain the concept of Continuous Random Variable and Discrete Random Variable. What is the CDF and PDF ? Plot PDF of uniform distributed random variable over an interval (0 to 2π). [7]