

- b) For a given system, $\dot{x} = \begin{bmatrix} 0 & -2 \\ 1 & -3 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$, $y = [1 \ 0]x$, $x(0) = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$
 Obtain $x(t)$ for unit step input. [6]
- c) Draw circuit diagram of op-amp based lead/lag compensator, write transfer function and draw pole zero plot. [4]

Q3) a) In a unity feedback system an ideal relay with output equal to ± 1 unit is connected in cascade with $G(s) = \frac{20}{s(s+1)(s+3)}$ Determine amplitude and frequency of limit cycle if it exists by describing function method. [10]

- b) Explain any one peculiar behavior of nonlinear system : [6]
- i) Jump resonance
 - ii) Limit cycle
 - iii) Sub-harmonic oscillations

OR

Q4) a) A linear second order system is described by equation. [10]

$$\ddot{e} + 2\xi\omega_n \dot{e} + \omega_n^2 e = 0$$

where, $\xi = 0.3, \omega_n = 1 \text{ rad/sec}, e(0) = 2, \dot{e}(0) = 0$.
 Construct the phase trajectory using method of isoclines.

b) Explain different types of singular points of the phase trajectories. [6]

Q5) a) Draw the block diagram of digital control system & explain the function of each block in short. [10]

b) Determine inverse Z transform of [6]

- i) $\frac{z^2 + 3z}{z^2 + 3z + 2}$
- ii) $\frac{(1 - e^{-3T})z}{(z-1)(z - e^{-3T})}$

OR

Q6) a) Explain the sampling and reconstruction process, State the sampling theorem and give its importance. [10]

b) Solve the following equation by using z-transform method. [6]
 $x(k + 2) + 5x(k + 1) + 6x(k) = 0$ where $x(0); x(1) = 1$

Q7) a) Define Pulse Transfer Function and obtain the pulse transfer function of two systems in cascade with sampler in between. [8]

b) Obtain the direct and cascade realization of [10]

$$D(z) = \frac{z^2 + 5z + 2}{z^3 + 6z^2 + 4z + 1}$$

OR

Q8) a) Write a short note on Digital PID Controller. [8]

b) Obtain the closed loop pulse transfer function of the following system. [10]

