

### C14-A-401/C14-AA-401/C14-AEI-401/C14-CH-401/ C14-CHST-401/C14-IT-401/C14-MET-401/C14-MNG-401/ C14-PKG-401/C14-TT-401/C14-C-401/C14-CM-401/

C14-EC-401/C14-EE-401/C14-M-401

## 4401

### **BOARD DIPLOMA EXAMINATION, (C-14)**

MARCH / APRIL - 2019

# COMMON - IV SEMESTER EXAMINATION ENGINEERING MATHEMATICS - III

Time: 3 Hours [Total Marks: 80

#### PART - A

3×10=30

Instructions:

- (1) Answer ALL questions.
- (2) Each question carries THREE marks.
- (3) Answer should be brief and straight to the point and shall not exceed five simple sentences.

1 Solve 
$$(D^2 + 2D - 3)y = 0$$

2 Solve 
$$(D^2 + 4D + 4)y = 0$$

3 Find the PI of 
$$(D^2 - 25)y = \sin 5x$$

**4** Find 
$$L(t^3 + \cos 3t + 3e^{2t})$$

5 Find 
$$L(t^3e^{2t})$$

$$\mathbf{6} \qquad \text{Find} \quad L^{-1} \left( \frac{s}{\left( s+3 \right)^2} \right)$$

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- 7 Find  $L^{-1}\left(\frac{3s+7}{s^2-9}\right)$
- **8** Write the Fourier series for the function f(x) in the interval  $(C, C + 2\pi)$ .
- 9 Calculate the coefficient  $a_0$  in Fourier series of expansion of x in (0,2).
- 10 If A, B are two disjoint events in a sample space S,  $P(A) = \frac{3}{5}$ ,  $P(B) = \frac{3}{4}$ , then find  $P(A \cup B)$ .

 $PART - B 10 \times 5 = 50$ 

Instructions:

- (1) Answer any FIVE questions.
- (2) Each question carries TEN marks.
- (3) Answer should be comprehensive and the criterion for valuation is the content but not the length of the answer.
- 11 (a) Solve  $(D^2 6D + 9)y = e^{3x} + \cos 2x$ 
  - (b) Solve  $(D^2 4D + 3)y = \sin 3x$
- **12** (a) Solve  $(D^2 + 1)y = x^2 + 7x + 9$ 
  - (b) Solve  $(D^2 + D 6)y = e^{-2x} + 5$
- 13 (a) Find  $L(e^{3t}\sin 3t\cos t)$ 
  - (b) Find  $L^{-1}\left(\frac{1}{s^2 3s}\right)$

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- 14 Using convolution theorem find  $L^{-1}\left(\frac{1}{s(s^2+4)}\right)$
- Develop  $f(x) = x^2$  in a Fourier series in the interval  $(-\pi, \pi)$  and deduce that  $\frac{1}{1^2} \frac{1}{2^2} + \frac{1}{3^2} \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$
- 16 Obtain the Fourier series for  $f(x) = x^2 2$  in the interval (-2, 2).
- 17 (a) If two cards are drawn at random from a pack of 52 cards, then find the probability for the cards to be one spade and one heart.
  - (b) If A and B are two independent events with  $P(A) = \frac{1}{3}$ ,  $P(B) = \frac{1}{2}$ , then find  $P(A \cup B)$  and  $P(A \cap B)$ .
- 18 Three urns have the following composition of balls

Urn I: 1 while, 2 black,

Urn II: 2 white, 1 black,

Urn III: 2 white, 2 black

One of the urns is selected at random and a ball is drawn. It turns out to be white find the probability that it come from urn III.