



C16-M-401

5684

BOARD DIPLOMA EXAMINATION, (C-16)

MARCH/APRIL—2018

DME—FOURTH SEMESTER EXAMINATION

ENGINEERING MATHEMATICS—IV

Time : 3 hours]

[*Total Marks : 80*

PART—A

$3 \times 10 = 30$

Instructions : (1) Answer **all** questions.

(2) Each question carries **three** marks.

1. Solve $(D^2 - 2D - 3)y = 0$.

2. Solve $(D^2 - D - 1)y = 0$.

3. Solve $(D^3 - D^2 - D - 1)y = 0$.

4. Find the PI of $(D^2 - 25)y = \sin 5x$.

5. Find the PI of $(D^2 - 6D - 9)y = e^{3x}$.

6. Find $L(t^3 \cos 3t e^{3t})$.

7. Find $L(e^{2t} \sin 3t)$

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- 8.** Find $L^{-1} \frac{s}{(s-2)^2}$.
- 9.** Write the Fourier series for the function $f(x)$ in the interval $(C, C+2)$.
- 10.** Calculate the coefficient a_0 in Fourier series of expansion of x in $(0, 2)$.

PART—B

$10 \times 5 = 50$

Instructions : (1) Answer *any five* questions.
 (2) Each question carries **ten** marks.

11. (a) Solve $(D^2 - 2D - 1)y = e^{3x}$.
 (b) Solve $(D^2 - D - 2)y = \sin 2x$.

12. (a) Solve $(D^2 - 1)y = x^2 - 2$.
 (b) Solve $(D^2 - 6D - 4)y - 4 = e^{2x}$.

13. (a) Find $L(e^{3t} \sin 3t \cos 2t)$.
 (b) Find $L(t^3 e^{2t})$.

14. (a) Find $L^{-1} \frac{1}{s^2 - 4s}$.
 (b) Find $L \frac{\sin 4t}{t}$.

15. (a) ^{*}Using convolution theorem, find

$$L^{-1} \frac{1}{s(s^2 - 9)}$$

(b) Using Laplace transform technique, find $\int_0^\infty e^{-3t} \sin 2t dt$.

16. Using Laplace transform method, solve $y' - y = t$, $y(0) = 1$, $y'(0) = 0$.

17. Develop $f(x) = |x|$ in a Fourier series when $x \in [-\pi, \pi]$. Hence deduce that

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$$

18. Obtain the Fourier series for $f(x) = e^x$ in the interval $(0, 2\pi)$.

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